Measurement of pressure and assessment of cavitation for a 22.5-kHz intra-arterial angioplasty device

I. R. S. Makin

E. Carr Everbach
Swarthmore College, ceverba1@swarthmore.edu

Follow this and additional works at: https://works.swarthmore.edu/fac-engineering

Recommended Citation
Measurement of pressure and assessment of cavitation for a 22.5-kHz intra-arterial angioplasty device

Inder Raj S. Makin and E. Carr Everbach
Swarthmore College, Department of Engineering, Swarthmore, Pennsylvania 19081-1397

(Received 29 August 1995; accepted for publication 24 March 1996)

This study was performed to understand better the mechanisms of action of an (22.5 kHz) ultrasonic wire catheter device used to remove atheromatous plaque in diseased blood vessels (ultrasonic angioplasty). During a clinical procedure, the wire acts as an acoustic waveguide to transfer acoustic energy from a generator outside the body to the ball tip of the wire, which is inserted in the blood vessel. The acoustic field radiated by the vibrating ball tip (1.5- to 3.0-mm diameter), was mapped in a relatively large (600 L) water tank and compared to the field from a well-characterized simple source. A dipolelike radiation pattern due to the translating ball tip was observed. At low power settings, standing wave effects in a smaller cylindrical volume (200-mm diameter, 350-mm height), which was used to simulate anthropometric dimensions, increase relative to the larger tank measurements. The standing wave ratio is dependent upon the $p_c$ characteristics of the medium and the dimensions of the volume, rather than on the absorption at this frequency. At high power settings of the device, cavitation at the tip of the wire was measured using a 20-MHz passive cavitation detection scheme. © 1996 Acoustical Society of America.

PACS numbers: 43.80.Sh, 43.80.Gx, 43.35.Ei [FD]

INTRODUCTION

Intensive research efforts are underway to control the high incidence of coronary arterial disease and the occlusion of the peripheral vasculature among the aging human population in western societies. One approach in treatment is the development of instrumentation that invasively removes the obstruction in the diseased vessel. Removal of atheromatous plaque (angioplasty) is currently achieved by a wide array of physical means such as vessel dilating balloons, laser beams, mechanical tissue removal devices, as well as low-frequency ultrasonic wires.\(^1\)\(^2\) However, as mentioned in Ref. 1, the various methods of angioplasty exploit two basic physical techniques of tissue repair, namely “remodeling” of the lumen by compressing the cholesterol plaque and “removal” of the occluding material. Ultrasound angioplasty falls principally in the latter device category, whereby the blocking material is physically removed from the underlying normal lining of the blood vessel.

Compared to competing angioplasty techniques such as laser angioplasty and mechanical atherectomy devices, the ultrasonic technique affords advantages in terms of more controlled and selective removal of the diseased fibrotic and/or calcified tissue layer, while sparing the underlying normal layers.\(^2\)\(^-\)\(^7\) In addition, the particle size of the ablated debris is sufficiently small to minimize the blockage of vessels downstream and is comparable to that produced by other therapeutic techniques.\(^2\)\(^,\)\(^7\) Hence the ultrasound modality entails comparable risks due to embolization (blockage) in the circulation comparable to that of current angioplasty techniques.

The description and the speculated mechanisms of the ultrasonic angioplasty techniques have so far been described mainly in the medical literature. The speculated mechanisms of action of these devices are based on the experience gained in a clinical setting for in vitro experiments, or in vivo animal or human studies. Only recently has a theoretical analysis of low-frequency ultrasonic devices such as the ones used for angioplasty been presented by Nyborg.\(^8\) It is believed that bubble growth and collapse caused by the acoustic field around the oscillating ball tip of the wire is a mechanism of action of the device.\(^2\)\(^,\)\(^8\)\(^,\)\(^9\) However, cavitation in the ultrasonic angioplasty system could possibly result from a combination of effects, namely, the acoustic field due to vibration of the wire tip as well as the pressure gradients around the tip caused by the hydrodynamic flow field. The hydrodynamics of a sphere moving through water will briefly be considered in Sec. III and the Appendix. The aim of this research is to perform direct pressure measurements of the acoustic fields emitted by the ultrasonic source in order to attain a better understanding of the radiation pattern of the source and, in addition, to gain a better understanding of the mechanisms of action of the device.

I. MATERIALS AND METHODS

A. Description of the device

The device under investigation [Alliger Ultrasonic Wire System (AUWS), MISONIX Inc., Farmingdale, NY] is being developed for a technique of disruption of atherosclerotic plaque and thrombi in the coronary and peripheral blood vessels by using sound energy. The functional components of the system are: a generator, convertor, damper, and the wire, as shown in Fig. 1. The generator supplies a high-voltage signal at 22.5 kHz to the piezoelectric crystals (PZT4) placed in the convertor. The acoustic energy radiated from the piezo elements is guided through a tapered stainless steel horn and conducted further into a titanium wire of variable length and thickness. The wire terminates in a ball tip and is encased in a Teflon® sheath. In order to restrict the transverse whipping of the wire during operation, a fluid
(preferably of high viscosity) is pumped under pressure (50–
100 psi) through the damper port and under the sheath cov-
ering the wire (see Fig. 1). The diameters of the ball tips for
the wires used in our experiments were 1.98 and 2.46 mm;
the wires’ respective lengths were 445 and 660 mm. The
measured amplitudes of displacement in the longitudinal di-
rection for the two wires at full operational setting of the
device were given by the manufacturer to be about 100 and
65 μm, respectively. The two wires described above and
investigated here will for simplicity be referred to as wires 1
and 2, respectively. The ball tip of wire 1 is mushroom
shaped.

B. Characteristics of the wire source

During operation of the device, sound is radiated into
the surrounding fluid mainly by the axial translatory motion
of the ball tip of the wire. Since the axial movement of the
ball tip (∼100 μm), as well as the radius of the ball tip (∼1.3
mm), are both much less than the wavelength of the driving
frequency in water (λ=66.6 mm for f = 22.5 kHz, c = 1500
m/s), the field radiated by the translatory movement of the
ball tip (see Fig. 2) may be approximated by that of a
dipole. Assuming that the radiation of sound from the ball
tip is dipolelike, a theoretical estimation of negative acoustic
pressures occurring at the tip can be made in order to predict
whether or not these pressures are sufficient to cause acous-
tic cavitation. For a ball tip of nominal radius a = 1.3 mm hav-
ing a maximum displacement d = 100 μm, the acoustic pres-
sure amplitudes expected at the wire tip are about 600 kPa—
sufficient to cause cavitation at the operating frequency of
22.5 kHz.8,10,11

As mentioned earlier, violent collapse of bubbles around
the tip of the wire is a possible mechanism of action of this
device. Cavitation could result during operation of the device
at high settings caused by acoustic pressure fields, as well as
the hydrodynamic activity around the wire tip. A brief dis-
cussion of the possible importance of hydrodynamic phe-
nomena in causing cavitation in the vicinity of the ball tip is
given in the Appendix.

The comparison of our experiments with theoretical pre-
dictions from a model of a translating sphere operating as a
dipole source can be qualitative at best since the model as-
sumes a free spherical body translating only in the z direc-
tion (refer to Fig. 2). In reality, however, a spherelike ball tip
is attached to a wire which has a tendency to whip trans-
versely.

C. Field measurements in a large volume

Measurement of the acoustic field from the ultrasonic
wire when it radiates in a relatively free field was performed
in the largest available tank, which measured 914×812×812
mm and was fabricated from 12.5-mm acrylic. However, sig-
nificant standing waves were still observed in the tank be-
cause of the relatively long wavelength of the signal and the
almost negligible attenuation of sound in water at 22.5 kHz.
The approach for assessing the field due to the unknown
source, i.e., the ultrasonic wire, was to compare its pattern
with the field due to a known simple source [Briel & Kjaer
(B&K) model 8103] operated at the same frequency, and
located at the same position as the wire in the tank. The tank
in each case was filled with water to the same level.

The experiments were controlled from a Macintosh Quadra 700 computer with a National Instruments GPIB in-
terface. In addition, the AUWS generator was activated from
the computer by a NBMO-16X D/A card. The programming
environment used to control various instruments and acquisi-
tion of data was LabVIEW (National Instruments). A sche-
matic of the experimental setup is shown in Fig. 3. Measure-
ment of the acoustic fields was performed by raster scanning
the horizontal and vertical planes symmetrically about the
source under investigation. The receiver used was a second
B&K 8103 hydrophone, which, according to the manufac-
turer, is a broadband, omnidirectional receiver in the 100-Hz
to 120-kHz range (<1-dB pressure deviation in the xz and
yz planes). The receiver is mounted on a computer-
controlled three-axis positioner (VELMEX Unislide lead
screw with NF-90 controller) as close to the source as pos-
sible and aligned end-on to the source under investigation.
The planes scanned were symmetric about the z axis (see
Fig. 3). Data points acquired for both the vertical and hori-
tzonal planes scanned the plane 150×150 mm about the z
axis, at a resolution of 3 mm. The resolution of 3 mm was
observed to be adequate for sources radiating a signal of
66.6-mm wavelength. The signal received at the B&K 8103

FIG. 1. Schematic of AUWS.

FIG. 2. Schematic of a translating sphere.

FIG. 3. Measurement setup for excitation of source and acquisition of re-
ceived signal.
hydrophone was amplified and filtered by a charge preamplifier (B&K model 2635) and recorded by a digital oscilloscope (LeCroy model 9450). The amplitude of the signal acquired by the scope was downloaded to the computer into a file.

As a first step, the accuracy of the B&K 8103 transducer as a simple source radiating at 22.5 kHz was tested. The source is pulsed with an eight-cycle toneburst at a pulse repetition frequency (PRF) of 5 Hz. The received signal measured is the amplitude of the direct wave signal launched from the source, such that any reflections from the tank boundaries are gated out. The measured pressure decay with range for the B&K 8103 source was in good comparison with the theoretically predicted pressure decay for a simple source Fig. 4(a). The scans in Fig. 4(b) and (c) show the smooth decay of pressure for the B&K 8103 source in the horizontal and vertical planes, symmetric about the z axis. The source is pulsed as described earlier.

The simple source (B&K 8103) is next driven in the continuous wave (CW) mode and its pressure field is measured, again, in the horizontal and vertical planes symmetric about the z axis. As in the case of the scans in the pulsed mode, the scanned planes extend from 21 to 171 mm in the z direction, and from −75 to 75 mm in the x or y direction. The step size between each measurement point is 3 mm.

The simple source is next replaced by the wire source. Although we expect a dipolelike radiation from this source, its field is complicated because of the transverse whipping of the wire. For these measurements, the wire is driven at very low power settings to minimize the influence on the field of the transverse motion of the wire. In addition, the low gain settings of the device allow the piezocrystals and the horn assembly to operate in their linear regimes. The acoustic fields for the two wires under investigation were measured in the form of horizontal and vertical planes extending between 12 and 171 mm along the z axis and −75 to 75 mm along the y and x axes. Due to the design geometry of the sources, the receiver hydrophone can be brought closer to the source in the case of the wires as compared to the B&K 8103 source used in the previous case.

Finally, for both the wires under investigation, the gain on the generator is turned up to a setting comparable to that used during a therapeutic procedure (dial settings of 13–14 on the generator). Measurement of acoustic pressures were made along the axis of the wire (z axis) from a range of 13 to 245 mm in step sizes of 2 mm. The received signal in this case is the amplified broadband response of the B&K 8103 transducer. The observed signal in the time domain is now erratic, the signal now having frequency components much higher than the 22.5-kHz driving frequency. The recorded pressure amplitudes correspond to the peak-to-peak pressure at a particular point noted at each instant in time.

D. Field measurements in a cylindrical tube

In the clinical setting, the ultrasonic wire is introduced through a peripheral blood vessel and operated within the body. It is relevant, therefore, to investigate the manner in which the acoustic field of the device varies when it is operated in a small volume. The scenario of the wire catheteriz-
transducer recorded passively the 20 MHz component of the broadband acoustic emissions of collapsing bubbles in the field due to the ultrasonic wire. A schematic diagram of the setup for the detection of cavitation is shown in Fig. 6. Briefly, the ultrasonic wire is positioned in a cell measuring 100×80×70 mm such that the distal tip of the ball on the wire is at the focus of the 20-MHz probe. The axis of the probe transducer is perpendicular to the axis of the wire. The cell is filled with deionized and degassed water. Since the cell is open to the atmosphere, the gas content of water attains equilibrium with the atmosphere prior to the experiment. The focus of the probe transducer is then moved beyond the ball tip by 1 mm along the z axis (see Fig. 6), with the help of a three-axis micrometer positioning stage on which the probe transducer is mounted. Since even at maximum operational settings, the longitudinal translatory amplitudes of the ball tip cannot be greater than 100 μm, shifting of the wire tip by 1 mm from the focus ensures that the signal received by the probe transducer is not a result of reflections from the surface of the wire tip. Any signal output at the 20-MHz transducer, therefore, is due to the violent collapse of individual bubbles and/or bubble clouds just distal to the ball tip of the wire. A broad bandwidth needle hydrophone is used simultaneously to monitor the noise in the megahertz frequency range emitted by collapsing bubbles close to the tip of the wire.

The 20-MHz probe is first driven in the pulse-echo mode and the ultrasonic wire is operated using a foot switch, the gain of the device being increased very gradually. Initially, no received signal at 20 MHz can be detected. However, as the gain on the AUWS generator is increased, a small steady signal at the location of the 20-MHz probe focus that is indicative of a bubble cloud forming at the tip of the wire can be detected. On increasing the gain on the wire generator further, the signal output at the probe increases in amplitude dramatically and becomes erratic in time. This response is indicative of violent collapse of bubbles, the sound resulting from which is being received by the probe at 20 MHz. Due to the continuous intense activity of bubble collapse at these gain settings of the generator, however, it is difficult to differentiate between the probe signal reflected from bubble clouds forming at the tip of the ball of the wire and the signal from violently collapsing bubbles. Therefore, the cavitation monitor is now switched to passive detection mode.

In passive mode, the probe transducer is not excited, functioning only as a narrow bandwidth receiver. The only

![FIG. 4. Comparison of theory for a simple source with experiment [(a)], and field maps for vertical and horizontal planes [(b) and (c)], for the B&K 8103 excited in the pulsed mode.](image)

![FIG. 5. Tube-in-tube model for field measurement in a bodylike space.](image)

![FIG. 6. Setup to measure cavitation during operation of the AUWS.](image)
FIG. 7. Comparison of fields radiating from a simple source and the wire source (wire 1) in the horizontal and vertical planes. Simple source: (a) and (c), wire source: (b) and (d).

FIG. 8. Field maps in horizontal and vertical planes for wires 1 and 2. Wire 1: (a) and (c), wire 2: (b) and (d).
signal that can be observed at 20 MHz in the current system is caused by the broadband signature of violent collapse of bubbles around the surface of the ball tip of the ultrasonic wire. The gain for the AUWS generator is maintained constant at a particular level. The device is then activated by the computer, and the acquisition of data from the 20-MHz transducer is initiated after allowing the AUWS time (about 5 s) to stabilize its output. The signal received as a result of cavitation at the ball tip is received by the 20-MHz transducer, amplified by a broadband receiver amplifier (MATEC model 625), and displayed on a digital oscilloscope (LeCroy model 9450). A root-mean square (rms) value for each screen display is calculated by the oscilloscope. These rms values are downloaded to the computer 3 to 5 times per second and stored in a file. After a predetermined duration (120 s), the computer turns off the AUWS and simultaneously stops any further acquisition of data. Details of passive estimation of cavitation activity in an intense sound field with the help of a narrow bandwidth focused 20-MHz probe is described by Everbach et al.14

II. RESULTS

A. Acoustic field in a large volume

As we described in Sec. I C, the field radiated by the AUWS is mapped in a relatively large tank, and is compared to the field from a simple source radiating in the CW mode in the same volume of fluid. Figure 7 shows a comparison of the fields in the horizontal and vertical planes, respectively, due to the two sources excited in the CW mode. The AUWS is operated at a low setting. We note a standing wave pattern in both cases due to reflections from boundaries of the tank. Important to note in these figures is the steeper decay of pressure with range in the case of AUWS source as compared to the simple source. The steep decay of pressure with range in the case of the AUWS source is indicative of its dipolelike radiation characteristic (note the pressure scales in Fig. 7). The pressure fields due to the wire source show a jaggedness as compared to the smooth simple source field. This jaggedness is caused by the transverse whipping of the wire even when it is operated at very low amplitude settings.

The field plots of the horizontal and vertical planes for wires 1 and 2 are shown in Fig. 8. Here the steep pressure decay close to the source becomes more apparent, since we now measure the field pressures starting closer to the source, i.e., from an axial range of 12 mm. We observe higher pressures in Fig. 8(a) as compared to Fig. 8(b). The gain settings on the generator in both cases were kept approximately the same. Since the pressure radiated from a source is dependent on its size,10,11 the higher output from wire 2 as compared to 1 can be explained by its larger source dimensions (ball diameter of wire 2 is 2.46 mm; wire 1 ball diameter is 1.98 mm). Similar to the horizontal plane measurements, the pressure field plots for both wires in the vertical plane [Fig. 8(c) and (d)] initially decay rapidly, followed by a slower decay in pressure. Differences in the horizontal and vertical plane fields are because of variations in the tank boundary impedances.

At high gain settings of the device generator, as shown in Fig. 9(a) and (c), the time signature recorded at 13 mm

![FIG. 9. Time waveforms [(a) and (c)], and axial field plots [(b) and (d)] for AUWS at high gain settings.](image-url)
from the wire tip is devoid of almost all periodicity and is quite complex. This complex signal is a result of the higher harmonics generated within the horn as well as the transverse whipping of the vibrating wire. In addition, significant jet formation is noted visually at the tip of the ball. The bubble activity further complicates the signal received at the hydrophone. Further, in Fig. 9(b) and (d) we note no standing wave pattern in the scans for peak pressures measured along the axis of the wire. On an average, the pressure is observed to decay monotonically with range. The acoustic pressures resulting at the surface of the ball tip extrapolated from the pressures measured on axis are at least a few atmospheres even with a conservative assumption of the pressure amplitudes varying inversely as range away from the wire source.

B. Acoustic field in a cylindrical tube

Measurement of the acoustic field radiated from the AUWS in a cylindrical space of about 11.5-liter capacity is a more appropriate approach in assessing the behavior of the device when it is operated within the human body. As described in Sec. I D, pressure measurements along the axis of the wire are made within a 12.5 mm polyurethane tube, inside which the ultrasonic wire is fixed.

Figure 10 shows the axial field plots for a water-filled cylinder with the central inner tube also filled with water. The source within the inner tube is a simple source vibrating at 22.5 kHz in Fig. 10(a), the sources for plotting the axial fields in Fig. 10(b) and (d) are the ultrasonic wires 1 and 2 being operated at a low gain setting. We note a much more distinct standing wave pattern in this case as compared to the field plots mapped with the corresponding sources in a much larger volume as discussed in Sec. II A. In addition to the smaller volume of the cylinder compared to the large tank discussed earlier, the field here is further differentiable from that in Sec. II A due to the cylindrical shape of the enclosure.

Comparing the fields from a simple source in Fig. 10(a) to the field due to the dipole-like radiation of the ultrasonic wire in (b) and (d), we note some difference in the position of nulls between the two scans. The peak amplitudes are different for the two source types, however, but important to appreciate here is the limited axial range-dependent decay in

![Image of Figure 10](image-url)
the pressure amplitudes and a dominance of the standing wave pattern when a source is radiating at a frequency of 22.5 kHz in water. On comparing Fig. 10(b) and (d), we note the output for the wire 2 to be higher than wire 1 for comparable gain settings of the generator. After removal of the central polyurethane tube and the top acrylic flange and repeating the scans described earlier in this section, no significant change in the standing wave pattern along the axis of the wire sources was observed (data not presented). Interfaces such as the 3.175-mm-thick acrylic walls of the cylinder are almost acoustically transparent to the 22.5-kHz signal in water, and in fact the signal experiences an almost pressure release boundary at the interface between the air and the walls of the cylinder. This observation is of practical relevance to the use of the AUWS within the body.

The axial acoustic field plots obtained on operating the AUWS at high amplitude settings for the wires 1 and 2 are shown in Fig. 10(c) and (e). The time signature of the signal was complex as in the case of measurements in the large tank [Fig. 9(a) and (c)], and comprised of frequency components much higher than the 22.5-kHz driving frequency. The peak pressure plots [Fig. 10(c) and (e)], show a much less significant standing wave pattern as compared to low gain settings of the device in (b) and (d). The less dominant standing wave character can be explained by the cancellation of the various modes, which are excited within the fluid volume when the source is radiating at multiple frequencies. The decay of pressure with range in this case, however, is not as marked as that observed in the corresponding measurements made in the large tank [Fig. 9(b) and (d)].

Finally, when the cylinder and the inside tube are filled with glycerin (results not presented here), we noted a marked decay of axial pressures with increasing range in addition to a standing wave pattern superimposed on the axial field. The normal modes which can be excited in the fluid filled cylinder now are different from those excited when it was filled with water, since the normal modes are a function of the sound speed of the medium. The decay of pressure in this case cannot be explained solely on the absorption of sound in glycerin. On pulsing the B&K 8103 simple source at 22.5 kHz successively in water and the 66% glycerin fluid, no measurable difference between the fields in the two fluids could be measured within the sensitivity of the system. Further, the measured value for the absorption coefficient of 100% glycerin at 1 MHz of 5.6 Np/m by Averkiou, can be extrapolated to 22.5 kHz by using an inverse quadratic frequency dependence and the value at 22.5 kHz is 0.0028 Np/m. Since we are using 66% glycerin, the absorption for the fluid is expected to be even smaller, and hence negligible at this frequency.

C. Measurement of cavitational activity

Even at very low gain settings of the AUWS, microbubbles are observed to form at the tip of the vibrating ball. As described in Sec. I E, the bubble cloud is observed by scanning the region just beyond the ball tip with a 20-MHz focused transducer and operated in the pulse-echo mode (data not shown).

For higher settings of the AUWS generator, when cavitational activity around the surface of the ball tip in the form of distinct bubble growth and collapse is established, the 20-MHz component of the sound due to collapse of bubbles is received by the detector transducer in the cell (described in Sec. I E and by Everbach et al.). Comparing the plots for wire 1 in Fig. 11(a) and (c), we note a dependence of the cavitational activity at the ball tip on the settings of gain on the AUWS generator. Further, as can be seen by comparing the left and right-hand column plots in Fig. 11, the amount of caviation occurring at the ball tip is dependent on the type of wire. Wire 1 is short, with a mushroom-shaped ball head, whereas wire 2 is longer with a larger, more spherical ball head. Cavitational activity is noted to be consistently higher at comparable gain settings for wire 1 as compared to the wire 2. The effect of using different wire types at different generator settings is summarized in Fig. 11(e). This effect is in contrast to the measurement of pressures at low gain settings of the AUWS where the output from wire 1 was observed to be lower than from wire 2.

III. DISCUSSION AND SUMMARY

The current study is motivated by the need to characterize a low-frequency intra-arterial angioplasty device currently under development for application in human patients. Since the device is driven acoustically, its effectiveness in practice could be enhanced by a better understanding of the manner in which the acoustic field generated by the device is distributed in a particular volume of fluid. Pressure measurements made with the wire device in a relatively large tank of water show a steeper rate of decay with range when compared with similar measurements made using a simple source, indicating a dipole-like radiation characteristic for AUWS. Further, as described in Sec. III B, both the wire sources as well as the simple source show a more marked standing wave pattern when operated in a small volume of fluid. The high standing wave ratio is a result of the long wavelength of the signal at 22.5 kHz in the fluid. At such low driving frequencies, the inter organ interfaces having reasonably well matched impedances can be treated as acoustically transparent to the signal. The principal mechanism for standing waves in the body (i.e., if they do occur), is probably the acoustic field reflected from the human tissue-air interface. Acoustic pressure varies with range, the operating conditions of the AUWS such as the high gain settings at which the device is used in practice, as well as the characteristics of the host medium.

Finally, based on calculations and measurements, the estimated pressures at the surface of the ball tip do result in
cavitation during operation of the device. In fact, cavitational activity has been hypothesized to be one of the principle mechanisms of action of such devices in causing disruption of atheromas.\textsuperscript{2,8} By operating the device at high gain settings, the occurrence of cavitation events based on the violent collapse of bubbles close to the surface of the ball tip was recorded. The amount of cavitation activity was measured for two representative wire tip configurations. The amount of cavitation due to the mushroom-shaped ball tip was observed to be greater than the one having a more spherical shape, although the acoustic pressure amplitudes for the larger ball tip were greater. The enhanced cavitation with the bluff mushroom-shaped wire tip as compared to the larger sized spherical wire is indicative of a hydrodynamic mode of occurrence of cavitation working in combination with cavitation due to the acoustic field. This issue has been briefly addressed in the Appendix. The occurrence of hydrodynamic cavitation probably becomes more significant at very high gain settings and for wire tip profiles with a sharper contour. Hence, if cavitation is indeed one of the principal mechanisms of action, then bluff shapes of ball tips could be expected to be more effective in a clinical setting than the smooth, spherical wire tips.

**ACKNOWLEDGMENTS**

This work was supported by an NSF Presidential Faculty Fellow award (Everbach), Number 9253777.

**APPENDIX: HYDRODYNAMIC CONSIDERATIONS**

In order to investigate the hydrodynamic phenomena, the ball tip is assumed to be spherical, the wire attachment at one end is ignored, and the movement of the spherical body is assumed to proceed in a non oscillatory manner, i.e., only along the \( z \) axis (see Fig. 2 for coordinate system). Based on the maximum displacement of the ball tip (\( \approx 100 \mu m \)), the maximum axial velocity is \( v_0 = 14.14 \text{ ms} \) at \( f = 22.5 \text{ kHz} \). The Reynolds number for the sphere can then be calculated as\textsuperscript{17}

\[ Re = \frac{\rho v_0 D}{\mu} \]

where \( \rho \) is the density of the fluid, \( \mu \) is the dynamic viscosity of the fluid, and \( D \) is the diameter of the sphere. This Reynolds number can then be used to determine the flow regime around the sphere, which in turn can affect the cavitation behavior.

![Figure 11](image_url)
\[
\text{Re} = \frac{\rho v a}{\mu} = 4.13 \times 10^4, \tag{A1}
\]

where \( a = 1.3 \text{ mm} \), and for water, density \( \rho = 1000 \text{ Kg/m}^3 \), and viscosity \( \mu = 0.89 \times 10^{-3} \text{ N s/m}^2 \). For flow around a sphere, the Reynolds number calculated in Eq. (A1) is sub-critical as compared to the high Reynolds number values which are associated with a sudden decrease in the drag coefficient.\(^{17,18}\) These drag forces result in a distribution of pressure magnitudes around the sphere much less than those predicted by theory for frictionless flow (about 1 atm).\(^{17}\)

Hydrodynamic cavitation occurs when the low fluid pressures are at or below the vapor pressure of the liquid. An estimate of the resistance of a flow system around a curved surface can be obtained by using the expression for the cavitation number \( \sigma \) (also called Euler’s number), which is defined as\(^{18-20}\)

\[
\sigma = \frac{P_0 - P_v}{\frac{1}{2} \rho v^2} = 0.97, \tag{A2}
\]

where \( P_0 = 1 \text{ atm} \) is the ambient static pressure, \( P_v = 0.03 \text{ atm} \) is the vapor pressure for water at 27 °C.\(^{21}\) A relatively high value of \( \sigma = 0.97 \) is indicative of inception of cavitation in the wake region of the sphere moving through water but not necessarily leading to violent cavitation\(^{19}\) as was observed physically with the device.

---

11 P. M. Morse, Vibration and Sound (American Institute of Physics, New York, 1986).