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Why Do Hills Look So Steep?

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Chapter 16
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INTRODUCTION

A pervasive illusion in normal human experience is the misperception of surface orientation or slant. An outdoor path that ascends a hill of some 5° is typically judged to be about 20° whether viewed from the top or bottom (Proffitt, Bhalla, Gossweiler, & Midgett, 1995). Conversely a hill that appears to be about 30° to the casual observer will typically turn out to be between 7° and 10° upon measurement. The magnitude of this error is illustrated in Figure II.16-1.

With experience, skiers, hikers, engineers, and other frequent viewers of measured hills become aware of this perceptual error and may learn to make more accurate verbal estimates. However, as far as is known, the underlying perceptual bias seems to persist (Durgin & Li, 2011a). In this chapter we consider several different forms of theory that have been proposed for understanding the overestimation of geographical slant in the context of summarizing relevant findings.

To begin with ecological considerations, note that the powerful force of gravity, including both its role in surface erosion and its role in toppling leaning structures, compresses the range of ground orientations with which humans are confronted. This fact is probably quite important to understanding why surface orientation can be systematically overestimated without much cost. The statistical distribution of surface orientations in the environment may, in fact, encourage the expanded coding of surface orientation (Durgin & Li, 2011a; Proffitt, 2006). The second point is that errors in the estimation of surface orientation do not depend exclusively on visual factors. Estimates of underfoot ground orientation while standing on a ramp, for example, show similar patterns of overestimation—even for congenitally blind participants (Hajnal, Abdul-Malak, & Durgin, 2011). Indeed, very steep ramps (i.e., 14°) can be judged even steeper under foot (haptically) than when regarded visually (Durgin et al., 2009; Hajnal et al., 2011). Spatial bias in the haptic perception of surface slant has recently been reviewed (Durgin & Li, 2012). This chapter focuses on visual slant perception while noting similarities and differences with haptic slant perception. Several of the phenomena discussed here, such as the effect of viewing distance on slant perception, are primarily relevant to vision.

Theories of slant overestimation have fallen into the two broad categories of teleological (or functional) theories and mechanistic (or incidental) theories. Functional theories have focused on several kinds of perceptual or behavioral advantages that might arise from the exaggerated coding or representation of ground orientation. In the natural environment, sensitivity to ground orientation might be used as a basis for recognizing one’s facing direction or location in a familiar geographic region (Nardi, Nitsch, & Bingman, 2010). It might also be particularly useful for taking energetics into account during route planning (Bhalla & Proffitt, 1999; Proffitt, 2006), and energy costs are highly relevant to coding the vertical dimension of space (Kammann, 1967). Perceptual error might even be used to more efficiently guide motor planning (Hajnal et al., 2011; Li & Durgin, 2012b) or simply to more efficiently represent the layout of the environment (Durgin & Li, 2011a; Durgin, Li, & Hajnal, 2010).

Incidental theories of slant misperception have included the idea that depth along the line of sight is foreshortened (Ross, 1974), which is sufficient to predict that uphill surfaces will appear too steep, that the perceived horizontal is altered in the presence of hills (O’Shea & Ross, 2007), or that perceptual biases tend to make surfaces appear more frontal than they are (Gibson, 1950). Each of these incidental theories has some measure of support, but none of them seem to fully account for the full range of observed perceptual biases. The incompleteness of these incidental theories has led some theorists to neglect their importance. But a full account of the overestimation of slant must take these facts into account as well.
This chapter argues for a hybrid theory of slant misperception that includes both functional and incidental components. Whereas the exaggeration of the vertical dimension has a clear value for layout recognition and route planning, it may be that a more general perceptual coding advantage supports both of these kinds of goals rather than privileging one or the other. The phenomenology of slant perception is relevant to this discussion.

CONSTANCY AND NONCONSTANCY IN SLANT PERCEPTION

Constancy refers to the ability of an organism to perceive one aspect of an object (such as slant) consistently despite irrelevant changes in viewing conditions (such as viewing orientation and optical distance). In this section we examine constancy and explain that there are at least two important respects in which the perception of slant is clearly not constant and three important respects in which it is surprisingly constant. In general, purely functionalist theories have limited resources for accounting for the failures of constancy described here, whereas purely incidental theories are often contraindicated by the presence of constancy.

Effects of Viewing Distance

As viewing distance from a hill surface increases, the perceived slant of the surface tends to increase (become more vertical), as illustrated in Figure II.16-2. This was demonstrated by Bridgeman and Hoover (2008) by having participants look at different fixation points along a hill of constant slope. At farther distances, perceived slants were greater. This effect is not due simply to a diminution of texture information in the distance or changes in perspective. The perceived orientations of large slanted surfaces (6°–36°) increase approximately linearly as a function of log distance even when gaze is straight ahead and monocular cues

![Figure II.16-2. For a farther observer, a hill will appear steeper. (a) An illustration of the empirically derived model of the effects of viewing distance on perceived slant (Li & Durgin, 2010, 2013). At each distance, slant judgments have a gain of about 1.5 (the function is primarily sinusoidal). (b) This one-parameter model fares well at predicting the hill estimation data of Proffitt et al. (1995): each white circle (in both graphs) represents the model prediction for a specific hill slant taking into account both its slant and the optical distance to hill for an observer at the base of the hill, viewing it with gaze forward. (c) The effect of distance generalizes to farther or nearer viewing: a hill of about 24° will be estimated as 42° when standing at the base (with gaze forward, the optical distance to the hill would be about 3.6 m) but as 48° when standing 10 m back from the base (i.e., 13.6 m from the hill surface at eye level).]
to distance are held constant using high-resolution virtual displays (Li & Durgin, 2010). This slope nonconstancy with distance can be measured with both explicit verbal estimates of slant and with implicit slant estimates based on judgment of perceived shape on the hill surface. That is, if an L-shaped configuration of balls is simulated on a hill surface and measurement is made of the perceived ratio between frontal and sagittal arms of the L, one can use trigonometry to compute the implied surface orientation relative to the line of gaze. Such computations turn out to be roughly consistent with verbal estimates, helping to confirm that the overestimation of slant is not simply a verbal error.

In the classic hill slant estimation studies of Proffitt et al. (1995), observers were asked to make slant judgments while viewing the hills with gaze forward and standing near the base of the hill. This means that shallow hills would have been observed at a much larger optical distance than steeper hills. For example, assuming an eye height of 1.6 m, a path of 5° would only reach eye level 18 m away, whereas, a steep embankment of 30° would reach eye level within 2.5 m. To address this confound, Li and Durgin (2010) conducted their study of effects of viewing distance. When viewing distance was kept fixed, the relationship between slant and perceived slant (in the measured range of 0°–36°) turned out to be well predicted by assuming that perceived slant increases with a gain of 1.5 relative to physical slant (Li & Durgin, 2010). In fact, a gain of 1.5 is consistent with the first quarter cycle of a sinusoidal function, which also seems to approximate the function that relates physical slant to perceived slant for small surfaces in reach (Durgin & Li, 2012; Durgin, Li, et al., 2010). Li and Durgin (2013) have further developed a sine-based model as illustrated in Figure II.16-2.

Panel (a) of Figure II.16-2 illustrates the principal features of the models developed by Li and Durgin (2010, 2013): At each viewing distance, the perceived slant functions have a gain of approximately 1.5, but the effective intercepts of the functions increase with the log of viewing distance. In this case we have plotted the slant functions for viewing distances associated with each of six of the hills tested by Proffitt et al. (1995), as well as noting the specific slant shown at each distance using the sine-based model of Li and Durgin (2013, Equation 3). Panel (b) of Figure II.16-2 replots these predicted points (and three others) along with the associated means and standard errors from Proffitt et al. Although the slant model was developed using virtual displays and implicit slant measurements (judging the aspect ratio of an L-shaped arrangement of balls on a hill surface), it provides an excellent fit to outdoor verbal estimation data.

This nonconstancy of perceived slant with respect to viewing distance is likely an incidental effect due to failure of stereoscopic depth scaling. Although textbooks typically discuss binocular disparity as a useful depth cue only for near space, disparity information can be useful out to nearly a kilometer for surfaces that are sufficiently extended in depth (such as hills), but the scaling of stereoscopic depth information is known to show poor constancy at far distances (Palmisano et al., 2010). Many people are aware of the fact that mountains in the distance look essentially vertical. What is harder to notice (though it is observable) is that the apparent slants of hills gradually become shallower as we get closer to them.

If we consider the various functional accounts of hill misperception, it is difficult to see how any of them is strengthened by the effects of viewing distance. Perhaps a landmark could be more readily noted if its slant is exaggerated with distance, but using slant to orient to the environment would seem, on the face of it, to demand more constancy rather than less. Similarly, a functional account in terms of energetics should have trouble accounting for nonconstancies. If a climbable slope seems insurmountable when viewed in the distance, this does not seem particularly useful for route planning. The only functionalist theory that seems to be directly compatible with distance effects (i.e., not contradicted by them) is the expanded coding theory. Coding theory only need imply that slants will be exaggerated to better act upon them. Within immediate action space (several meters), the nonconstancies are both minor and fully predictable.

Failures of Constancy as Optical Slant Decreases

Li and Durgin (2009) found that downhill slants show a noticeable failure of constancy, depending on viewpoint. Using controls for viewing distance, Li and Durgin reported that downhill slants appeared steepest when the direction of view is nearly parallel to the hill surface, such as when our gaze first crests them. Many skiers have confirmed the basic observation that a downhill slope appears less steep as one gets closer to the edge. Some report that they try to minimize the sense of danger by initiating the process of launching themselves onto the hill before they have fully crested it. The apparent steepening of the hill at the point where gaze is nearly parallel with the surface may serve to signal uncertainty or risk, but it nonetheless appears to be an incidental effect rather than primarily functional because the steepening effect for downhill slants has a corresponding effect for uphill slants: When gaze is nearly parallel to slant, the visual system tends to treat gaze direction itself as the sole estimate of slant (Durgin & Li, 2011a). This effect has been observed for real and simulated downhill surfaces (Li & Durgin, 2009) as well as for small uphill simulated surfaces viewed at shallow optical slants, with gaze nearly parallel to the surface orientation (Durgin & Li, 2011a).

Evidence for Constancy With Viewing Direction

A surprising amount of constancy is evident in slant perception with respect to the lateral direction of gaze. Proffitt, Creem, and Zosh (2001) showed that, even when people looked at a hill from an oblique perspective, participants’ estimates remained exaggerated. Proffitt et al. did not control for viewing distance, but their data strongly suggest that the encoding of three-dimensional slant provides substantial constancy with respect to direction of observation. For smaller, uphill surfaces, Durgin, Li, et al. (2010) reported an impressive amount of constancy as well with changes in the pitch of gaze, suggesting that coding biases in slant perception affect geographical slant (slant relative to gravity) rather than optical slant (slant relative to the line of sight). As shown in Figure II.16-3a, Durgin, Li, et al. had participants estimate the slants of small surfaces either with gaze forward or with gaze declined by nearly 45°. If slant misestimation were due primarily to distance foreshortening along the line of sight (also known as “frontal tendency”), then a board at about 60° from horizontal
should seem steeper with gaze forward (Fig. II.16-3a, right) than with gaze downward (Fig. II.16-3a, left), but no substantial differences were found. The function relating perceived slant to actual slant can be approximated by a sinusoid for slants within arm’s reach (Li & Durgin, 2013). This effect is not verbal/numeric: the same spatial bias occurs whether numeric estimates are made relative to vertical or to horizontal. Moreover, when a forced-choice procedure was used to measure the bisection point between vertical and horizontal, surfaces of about 34° from horizontal were judged as being 45° (from horizontal and from vertical).

**Evidence for Constancy Across Surface Size**

Although slant illusions are less dramatic for near surfaces at eye level, in the range of slants between 0° and about 50°, perceived orientation is expanded with a gain of about 1.5 (Durgin & Li, 2011a). This same 1.5 gain function is evident in the models of large-scale slants discussed previously. That is, the perceived orientation of small real surfaces presented under full-cue conditions are expanded in the lower half of the range by a factor of about 1.5, and exactly the same scaling factor applies to large-scale hills. Thus the perceived orientation of large-scale surfaces seems to be no different, with respect to bias, than the perceived orientation of smaller-scale surfaces. The success of the sine-based model in capturing both the hill data and the data from small surfaces shows that there is no discontinuity between small and large surfaces in slant misperception (Li & Durgin, 2013). This point, again, is consistent with the expanded coding theory because it points to a generalized coding scheme that applies to slant in general rather than exclusively to landmarks or to intended paths of travel.

**Evidence for Constancy Across Modalities**

As reviewed by us elsewhere, a sine-based model can apply to haptic surface perception by hand as well (Durgin & Li, 2012) and even to proprioception of hand orientation (Li & Durgin, 2012b). Thus the underlying spatial bias function in slant perception seems to be multimodal. Even in the cases that seem exceptional, further analysis suggests good calibration between modalities. For example, Durgin et al. (2009) reported that verbal estimates of a 14.5° ramp were only 26° when based on visual inspection of the ramp while standing near the base (and looking down), whereas estimates from haptic information while standing on the ramp were closer to 31°. The second (haptic) estimate corresponds well with the sine-based model estimate of visually perceived slant for a 14.5° hill when viewed with gaze forward from the base (with a viewing distance to surface of about 6.5 m). In other words, if a person were walking up such a hill and simultaneously viewing the hill with gaze forward, the visual perception of slant and the haptic perception would be aligned (both would be about 31°). In contrast, the 26° estimate can be arrived at by using the actual viewing distance to the ramp surface (about 2 m) in the model.

**Summary of Slant Constancy**

The evidence we have reviewed here suggests that perceived slant shows marked failures of constancy with viewing distance and with certain extreme directions of gaze with respect to surface orientation. In contrast, visually perceived slant is remarkably constant across most changes in viewing orientation, across different scales of surface size (when viewing distance is taken into account), and across different modalities. Perhaps the most significant fact about the systematic biases in slant perception is that these biases seem to be coded primarily with respect to the extrinsic reference frame specified by gravity (Durgin, Li, et al., 2010) though some incidental effects indicate that there are also consistent biases with respect to optical slant as well.
SOCIOCOGNITIVE FACTORS IN THE EVALUATION OF SLANT

A number of reports have been made suggesting that slants look steeper to people for whom they represent a greater challenge to scale. Factors that have been reported to affect the evaluation of slant include age, fitness, encumbrment, fatigue (Bhalla & Proffitt, 1999), fear (Stefanucci, Proffitt, Clore, & Parekh, 2008), social support (Schnall, Harber, Stefanucci, & Proffitt, 2008), and blood sugar (Schnall, Zadra, & Proffitt, 2010). These various studies have been critiqued extensively (Durgin et al., 2009; Durgin, Hajnal, Li, Tonge, & Stigliani, 2010, 2011; Durgin, Klein, Spiegel, Strawser, & Williams, 2012; Durgin, Ruff, & Russell, 2012; Shaffer, McManama, Swank, & Durgin, 2013). In some cases, such as a study of the elderly, the originally published data actually contradicted the hypothesis: The elderly gave lower estimates for hill distances, but this was not made evident in the initial report. In other cases, such as a study of fitness, confounding factors (e.g., sex differences in slant estimation) were not taken into account in the analyses (see Durgin, Hajnal, et al., 2010 for a discussion). In yet others concerned with fear, subjects may have been excluded from analysis in a manner that inadvertently biased the results (see Durgin et al., 2009, for a discussion).

The critiques of the studies of encumbrment are worth reviewing briefly here. If participants in a study are simply asked to wear a heavy backpack, they tend to give higher estimates for hills than do nonencumbered participants. However, they also tend to report that they thought the backpack was supposed to make the hill look steeper (Durgin et al., 2009; Durgin, Klein, et al., 2012). If the backpack is instead presented as carrying equipment essential to the conduct of the experiment (Durgin et al., 2009; Durgin, Ruff, et al., 2012; Shaffer et al., 2013), or participants are told not to let themselves be influenced by the backpack (Durgin, Klein, et al., 2012), the judgments that they give tend to be identical to those of nonencumbered participants. In general, the use of heavy backpacks that are transparently intended to increase estimates of slant seem to produce social pressure on participants to elevate their slant estimates. Susceptibility to that social pressure can be mitigated by social support (Schnall et al., 2008) and may be exacerbated by low blood sugar (Durgin, Klein, et al., 2012; Schnall et al., 2010; Shaffer et al., 2013). Durgin, Klein, et al. (2012) found that the effects of blood sugar disappeared when participants were simply told to ignore the heavy backpack they were required to wear during such studies. Shaffer et al. (2013) showed that low blood sugar produces opposite effects (lower estimates) if participants believe the drink (which they assume contained sugar) was supposed to make the hill look shallower. Disputes over these sorts of controversial findings remain lively in the literature (e.g., Firestone, 2013). It is very clear that social compliance can have powerful effects on judgments and should be taken into consideration in studies that are ostensibly of perception.

The idea that slant overestimation provides a means for the direct perception of the energetic affordances of the environment (Proffitt, 2006) is quite a clever one. However, much of the evidence amassed in support of this theory has proven problematic, and no direct connection seems to exist between energetics and slant perception (e.g., Shaffer & Flint, 2011). A surviving tenet of this view, however, is that geometric accuracy might not be the proper goal of perceptual representation. This is also a tenet of expanded scaling theory, and if the exaggeration of perceived slant incidentally helps people to more reliably evaluate the energetic affordances of the environment for the purpose of route planning, so much the better.

THE ROLE OF THE PERCEIVED DIRECTION OF GAZE

Because slant is defined relative to a gravitational reference frame (i.e., the horizontal plane and the vertical vector of gravity that is normal to horizontal), errors in perceived slant could come about if the presence of a hill produced a distortion in the perception of the horizontal plane. O'Shea and Ross (2009) have provided evidence for such effects in the presence of large-scale mountains (see also Matin & Li, 1992), and Ooi and He (2007) have suggested that the ground plane itself is perceived as being tilted upward. The magnitude of such effects, however (about 3°–5°), is insufficient to account for the very large magnitudes of distortion in perceived slant.

Recently a much more dramatic distortion in perceived gaze direction has been documented that seems more consistent with the overestimation of slant. Specifically, much as the perceptual gain for perceived slants (less than 45°) is about 1.5 when distance is fixed, Li and Durgin (2009; Durgin & Li, 2011a) have used a variety of methods to document that the perceived declination of gaze is also coded with a gain of about 1.5. Durgin and Li (2011a; Li & Durgin, 2012a) have proposed that angular variables relevant to the pitch axis are coded on an expanded scale so as to increase their precision because they are highly relevant for action.

Gaze declination relative to the horizon is a powerful cue to distance (Messing & Durgin, 2005; Ooi, Wu & He; 2001; Sedgwick, 1986; Wallach & O'Leary, 1982), because on level ground (and most of the spaces we deal with are within 5° of level) it provides highly reliable proprioceptive cue to ground distance. Given the bandwidth limitations of neural transmission, coding this angular variable on an expanded scale would preserve greater precision relevant for the control of action. Thus a functional account of slant overestimation derives in part from the idea that angular distortions are present in perceptual experience in order to maintain precision for action. The expanded scaling of perceived gaze declination has been measured implicitly (Durgin & Li, 2011a; Li & Durgin, 2009) based on slant estimates viewed along different lines of sight; it has been measured directly with balls suspended in the air or placed along the ground, and it has been measured by means of a bisection task (Durgin & Li, 2011a; see also Durgin & Li, 2011b). In all cases the gain was found to be approximately 1.5. Studies of verbal distance estimation among nonexperts tend to suggest linear compression of perceived ground distance by a factor of 0.7 to 0.8 (Loomis & Philbeck, 2008), consistent with a misperception of gaze direction, as illustrated in Figure II.16-4a. Rather than hills looking steep because of distance foreshortening, it may be that ground distances are underestimated because crucial
the grade of the hill is 31% (a 100% grade would be a 45° slope). Since 15° is simply unbelievable for anyone who has been to Lombard Street, many websites simply report this as 31° (which still seems too low compared to the perceptual phenomenology). The hill is so steep that Lombard Street winds back and forth across it so as to reduce the effective slant of the road to 10°—still quite steep when walking up it!

As Marr (1982) pointed out, there are many different forms of answers to questions about explanation, including the functional and the mechanistic. This chapter has considered the phenomenology of hill perception while discussing a variety of theories that have been proposed. One answer to the question in the title might remain the one put forth by Kammann (1967): because of gravity. The environment in which we have evolved is laid out such that vertical extents and slants are relatively tiny compared to horizontal extents. Expanding the vertical scaling of such an environment might produce many cognitive advantages, even if that expansion is done in angular terms. A second, mechanistic answer remains: because of a loss of reliable information for depth along the line of sight. This latter answer addresses the failure of slant constancy with changes in viewing distance, but it cannot be the whole story, because it does not account for the misperception of downhill slant or the relative constancy of perceived slant with large changes in angle of regard. This chapter has emphasized that the misperception of hills is probably part of a larger family of biases in the perception of angular variables that includes the misperception of small surfaces in reach and may even include the misperception of ground distance and height based on multiplicative biases in perceived angular deviations of visual direction from horizontal.

Although this review has taken sides on some controversies, there is not room to address controversies over the interpretation of different measurement techniques for evaluating perceived slant (e.g., Coleman & Durgin, 2014; Creem & Proffitt, 1998; Durgin, 2013; Durgin, Hajnal, et al., 2010; Durgin, Li, et al., 2010; Li & Durgin, 2010, 2011, 2013; Shaffer, McManama, Swank, Williams, & Durgin, 2014; Stigliani, Li, & Durgin, 2013; Taylor-Covill & Eves, 2013; Witt & Proffitt, 2007). These controversies focus around the question of whether using a haptic matching task to measure slant provides a route to a separate (undistorted) dorsal stream representation.

It is therefore worth making one final point about the nonconsequences of slant misperception. Our actions seem effective in a perceptually distorted world as everything else (Powers, 1973). This means that acting with accuracy in a perceptually distorted space is not only downhill slant perception (Li & Durgin, 2009; see Fig. II.16-3, bottom) but also systematic errors in the comparison of distance and height. For example, Higashiyama and Ueyama (1988) developed a task requiring participants to place themselves at the same distance from objects (such as poles) as those objects were high. Participants placed themselves much too far away, as illustrated in Figure II.16-4b. Li, Phillips, and Durgin (2011) recently replicated this experiment and extended it to show that the exact pattern of results reported by Higashiyama and Ueyama could be predicted by a parameter-free geometric model in which the previously measured angular declination gain of 1.5 was assumed. This suggests that hill misperception is part of a larger pattern of angular distortions that affect the perception of surface layout generally.

**Why Do Hills Look So Steep?**

Slant misperception is dramatic. An editor at a journal once challenged the statement that Lombard Street in San Francisco is on a hill that is only 15° in slope. He said he had checked the Internet and found that the true value is 31°. He was correct that many sites on the Internet report a value of 31°. In fact, the tangent of 15° is 0.31, and so
answer to why hills (and even small surfaces in reach) look so steep is therefore: Why not?

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